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	Block diagram of He- Neaton.
·	working Principle:
. 10	For this lover system a guartz tube is filled with a pulature of
	He & Ne gases en the rateo 10:1 respectively at a pressure of
	about oil mon of Hg. This nexture ack as the active medium.
	Hérs numped up to the excited state of 20.61 eV by electric
	discharge. Here, the excited level of Helium at 20.61 eV is Very
1	15 close to a level in neon at 20.66 ev-It is so close that upon
	collision of a He fine atom the energy can be transferred from
	Hellun to Neon atoms. Thus, the excelled Hellum atom does not
	returns to it's ground state by spontaneously emitting photons,
	rather, they transfer their energy to the Neon atoms through
2	o collescon. Such a transfer of energy can take place when the two
-	colleding atoms have identical states. Thus, He atoms helps
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	present in the entetactable statt. This way, we get other photons
	that are in phase with the stimulating photons. These photons
	are reflected back of forth by the silvered ends of the no. of photon
	ges annplified through stimulated entession everytime. Finally,
	a portron of these entiresited photons passes through the

11 1 Date portally silvered and as an output. 19/11/19 (Tutorial) How many photons of yellow light of A=5500A constitute 1.55 of energy nhv = 1.5NX 6.626×10-34 × 3×10° =1.5. 5500×10-10 N= 1.5×5500×10-0 6.626×10-34×3×10° 1.5×55×10 8434-8 = 4.15×10+18 6.626 X3 calculate the wavelength of a photon of Energy 5×10=19J. 5×10-19= hc A A= 6.626×10-34×3×108 5×10-19 -34+19.48 = 6-626×3 ×10 5 -34+**2**7 3.975×10 M = 3.975×10 m A = 3975 Å ≈ 4000 Å. 3. Is it possible to liberate an electron from a metal surface having work function 4.8 er with an incident radiation of 30 wavelength - (1) 5000 Å (1)2000Å

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ARYAN Page No Date 18) hc = 12406 eN = 2.48 eN (NOF possible) 5000 A 31 6.2 en (Possible) -(11) 2000 5 Find the morennum KE of the emilled electrons and the stopping potential of the light of wavelength 5890Å is incident on the surface for which threchold & wavelength is 7320Å. KEMOR = BNS. hc -hc 10 20 2 WE= KENLOO 12400×1430 1 KEMON = 12400 7320 589×732× 5890 = 0.4112 eV. = 0.4112×1.6×10-19J. = 0.657 ×10-19 KEWONE 6.57×10-20 J evs = KE VS=KE = 000 004112×1.6×16-195 1-6×10-19 V5 = 0-4112 OV The threshold wavelength for photo electoric emession in Tungstin is 2300 Å · what wavelength of light must be used in order for 30 dectrons with a moalman chirgy of 1.5ev to be ejected?

ARVAN Page No. E=12400 ev 1 1 Date A(A) \$= hc - KEWDA A 12400 ev= 12400 - 105 eV 2300 2 5.39+1.5 6-89= 12400 2 2= 1800A 6. 10 calculate the work function, stopping potential of maximum velocity of the a photodedron for light q- 2=4350° when it is incident on sodium surface consider the threshold wavelingth of photoelectrons to be 5420 A. OZhV-hV Ø=hvo D=hc AD = 2.28 eN . = 12400 4350.43 5420 = 2.28×1.6×10-19J $\phi = 3.66 \times 10^{-19} J$ KEMON= hV-hVo = 12400/1 5420, 4350 = 12400×1070 = 0.562×10-195 4350×5420 = VS = 0.562V eVS=KEMOR

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ARYAN Page No. 1 Date $\frac{1}{2} \frac{1}{2} \frac{1}$ Nm²= 0.562×2×10⁻¹⁹ ×1.06 9.1×10⁻³¹ = 004235×10+12 VAX = 00351×106 MJS. = 0°1976×1012 Nm = 0.4445×106 mls.

PH 113 Physics

Nuclear Shell Model

By **Nishi Srivastava** Department of Physics

Nuclear Shell Model

Definition

In nuclear physics, the **nuclear shell model** is a theoretical model to describe the **atomic nucleus (in terms of energy levels).**

- The nuclear shell model was proposed by Dmitry Ivanenko in 1932 and further developed independently by several physicists such as Maria Goeppert-Mayer, Eugene Paul Wigner and J. Hans D. Jensen in 1949.
- □ It must be noted this model is based on the Pauli exclusion principle to describe the structure of the nucleus in terms of energy levels.

The important features of nuclear shell model are:

- The Shell Model is partly analogous to atomic shell model which describes the arrangements of electrons in an atom.
- The nucleons move randomly in a nucleus and collide into each other frequently in liquid drop model. The shell model suggests that each nucleon in a nucleus moves in a well defined orbit and hardly makes any collision. This is why this model is also called as independent model..

- As Nuclear Shell Model is analogous to atomic shell model so filled shells results in greater stability
- The nucleons in a nucleus obey Pauli exclusion principle(no two nucleons may occupy same state at the same time). The neutrons and protons are treated separately when their states are considered. Each have its own array of available quantized states.
- In this model each nucleon is assume to exist in shell just like in atomic model.
- > The nuclei shell are associated with certain Magic Numbers.

Magic Number

In nuclear physics the magic number is the "Number of nucleons (either protons and nuetrons) such that are arranged into complete shell withen the atomic nucleus.

The seven most widely recognize magic numbers are 2,8,20,28,50,82,126.

The magic nuclei have special stability.

- If neutron (or proton) corresponds to magic number then we need greater energy to remove last neutron(or proton) which is called Separation Energy.
- If both proton and neutron corresponds to magic number then they are most stable nuclei.
- If number of neutrons corresponds to magic number then we have greater number and stable isotones.

- If number of protons corresponds to magic numbers then we have greater numbers and stable isotopes.
- i.e Calcium has six isotopes.
- > The element whose Z and N is a magic number has abundance.

B. E Curve



Nuclear Shell Structure



Merits of Shell Model

- 1. It explain the magic number.
- 2. It explain the magnetic moment of some nuclei.
- 3. It explain successfully ground state spin.
- 4. It explain the greater stability and high Binding energy

Limitation of Shell Model

- The first limitation that one notices is that there is a difference between shell-model wave functions and the real state of the nucleus.
- Apart from this, the large value of the quadrupole moment seen in many nuclei is hard to explain using this method.
- The strong-spin orbit interaction cannot be applied using this method.
- The shell model has limited applications and cannot be applied to heavy nuclei.

PH 113 Physics

Nuclear Fission and Fusion

By **Nishi Srivastava** Department of Physics

Binding Energy

A binding energy is generally the energy required to disassemble a whole system into separate parts. It is known the sum of separate parts has typically a higher potential energy than a bound system, therefore the bound system is more stable. A creation of bound system is often accompanied by subsequent energy release.

Nuclear Binding Energy

The component parts of nuclei are neutrons and protons, which are collectively called nucleons. The mass of a nucleus is always less than the sum masses of the constituent protons and neutrons when separated. The difference is a measure of the nuclear binding energy which holds the nucleus together. According to the Einstein relationship $(E=m.c^2)$ this binding energy is proportional to this mass difference and it is known as the mass defect.

Nuclear Binding Curve

If the splitting releases energy and the fusion releases the energy, so where is the breaking point? For understanding this issue it is better to relate the binding energy to one nucleon, to obtain nuclear **binding curve**. The binding energy per one nucleon is not linear. There is a peak in the binding energy curve in the region of stability near iron and this means that either the breakup of heavier nuclei than iron or the combining of lighter nuclei than iron will yield energy.

Nuclear Binding Curve

The reason the trend reverses after iron peak is the growing positive charge of the nuclei. The electric force has greater range than strong nuclear force. While the strong nuclear force binds only close neighbors the electric force of each proton repels the other protons.



Nuclear Fusion

In nuclear physics, nuclear fusion is a nuclear reaction in which two or more atomic nuclei collide at a very high energy and fuse together into a new nucleus, e.g. helium. If light nuclei are forced together, they will fuse with a yield of energy because the mass of the combination will be less than the sum of the masses of the individual nuclei. If the combined nuclear mass is less than that of iron at the peak of the binding energy curve, then the nuclear particles will be more tightly bound than they were in the lighter nuclei, and that decrease in mass comes off in the form of energy according to the Albert Einstein relationship.



Nuclear Fusion

Fusion reactions have an energy density many times greater than nuclear fission and fusion reactions are themselves millions of times more energetic than chemical reactions.

The fusion power offers the opportunity of an almost inexhaustible source of energy for future, but it the fusion technology presents a real scientific and engineering challenges.

Deuterium-Tritium Fusion

The fusion reaction of deuterium and tritium is particularly interesting because of its potential of providing energy for the future.

3T (d, n) 4He

The reaction yields ~ 17 MeV of energy per reaction.

Nuclear Fission

Nuclear fission refers to the splitting of an atomic nucleus into two or more lighter nuclei. This process can occur through a nuclear reaction or through radioactive decay. Nuclear fission reactions often release a large amount of energy, which is accompanied by the emission of neutrons and gamma rays (photons holding huge amounts of energy, enough to knock electrons out of atoms).

Types of Nuclear Fission

- **Spontaneous Fission**: Nuclei consisting of protons, electrostatic force of repulsion between them exceeds the nuclear binding force hence nuclei undergoes spontaneous fission
- Induced Fission: When neutron is bombarded on heavy nucleus it makes nucleus unstable this unstable nucleus undergoes fission and split into two fragment. Such fission is called as induced fission.

PH 113 Physics

Liquid Drop Model

By **Nishi Srivastava** Department of Physics

Models of Nuclear Structure

- •Why is the binding energy per nucleon almost constant?
- •Why do certain nuclei emit α -and β -particles through these particles do not exist inside the nucleus?
- •Why are the nuclei containing 2, 8, 20, 28, 50, 82 nucleons most stable?

•Like any other quantum mechanical system, a nucleus also exist in its excited states. The most stable state is the ground state in which the nuclei are generally found.

Models of Nuclear Structure

- The precise nature of the forces acting in the nucleus is unknown.
- Nuclear model are resorted to for investigation and theoretical prediction of its properties.

Models of Nuclear Structure

- Such models may be based on
 - the extrinsic analogy between the properties of atomic nuclei and those of a liquid drop

 \succ the electron shell of an atoms etc.

• The corresponding models are called the liquid drop model and shell model.

Liquid Drop Model

- The Liquid Drop Model was proposed by the Neils Bohr who observed that there are certain marked similarities between an atomic nucleus and a liquid drop.
- In the Liquid Drop Model, the forces acting in the nucleus are assumed to be analogical to the molecular forces in a droplet of some liquid.

Assumptions

- The nucleus is supposed to be spherical in shape in the stable state, just like as liquid drop is spherical due to the symmetrical surface tension forces.
- The forces of surface tension acts on the surface of the liquid drop. Similarly, there is a potential barrier at the surface of the nucleus.
- The density of a liquid drop is independent of its volume. Similarly, the density of the nucleus is independent of its volume.

Assumptions

- The intermolecular forces in a liquid are short range. Similarly the nuclear forces are short range forces.
- The molecules evaporate from liquid drop on raising the temperature of the liquid due to their increased energy of thermal agitation. Similarly, when energy is given to a nucleus by bombarding it with nuclear projectiles, a compound nucleus is formed which emits nuclear radiations almost immediately.
- When a small drop of liquid is allowed to oscillate, it breaks up into two smaller drops of equal size. The process of nuclear fission is similar and nucleus breaks up into two smaller nuclei.

Semi-Empirical Formula

Using the model of the nucleus as a liquid drop, we attempt to calculate nuclear binding energies.

There are five contributions to the binding energy:The volume energy is proportional to the number of nucleons.

•The surface energy is the reduction in the binding energy due to nuclear surface effects.

•The Coulomb energy is the repulsion between protons.

•The asymmetry energy is a reduction in binding energy which occurs when there are more neutrons than protons, and vice versa.

• The pairing energy is somewhat of a "fudge factor" which accounts for stability of even-even and evenodd nuclei, and the reduction of stability for odd-odd nuclei.

Volume Energy



As a first approximation, we can think of each nucleon in a nucleus as interacting solely with its nearest neighbors.

Energy associated with each nucleonnucleon bond = U

Because each bond energy is shared by two nucleons therefore each has a binding energy of ½ U.

When an assembly of spheres of the same size is packed together into the smallest volume, each interior sphere has 12 other spheres In contact with it



In a tightly packed assembly of identical spheres, each interior sphere is in contact with 12 others

Volume Energy

Hence each interior nucleon in a nucleus has a binding energy of =12(1/2U) = 6U.

If all A nucleons in a nucleus were in the interior, the total binding Energy would be

Or

 $E_v = 6AU$

$$\mathbf{E}_{\mathbf{V}} = \mathbf{a}_{1} \mathbf{A}$$
 Volume energy

Surface Energy

Actually, of course, some nucleons are on the surface of every Nucleus and therefore have fewer than 12 neighbors.

Surface energy \propto surface area $\propto 4\pi R^2$ If $R = R_0 A^{1/3}$ then Surface energy $\propto 4\pi R_0^2 A^{2/3}$ Or

Surface energy = - $a_2 A^{2/3}$

Surface energy \propto A^{2/3}



A nucleon at the surface of a nucleus interacts with fewer other nucleons than one in the interior of the nucleus and hence its binding energy is less. The larger the nucleus, the smaller the proportion of nucleons at the surface

Coulomb Energy

The repulsion between each pair of protons in a nucleus also contribute toward decreasing its binding energy.

The coulomb energy E_C of a nucleus is the work that must be done To bring together Z protons from infinity into a spherical aggregate The size of the nucleus.

$$V = -\frac{e^2}{4\pi\varepsilon_0 r}$$

Since there are Z(Z-1)/2 pairs of protons,

$$E_{C} = \frac{Z(Z-1)}{2}V = -\frac{Z(Z-1)e^{2}}{8\pi\varepsilon_{0}}\left(\frac{1}{r}\right)_{av}$$

Coulomb Energy

Where $\left(\frac{1}{r}\right)_{av}$ is the value of 1/r averaged over all proton pairs.

If the protons are uniformly distributed throughout a nucleus of radius R, $\left(\frac{1}{r}\right)_{av}$ is proportional to 1/R and hence 1/A^{1/3}

Therefore

$$E_{c} = -a_{3} \frac{Z(Z-1)}{A^{\frac{1}{3}}}$$

The Coulomb energy is negative because it arises from an effect that opposes nuclear stability.



The binding energy per nucleon is

$$\frac{E_{BE}}{A} = a_1 - \frac{a_2}{A^{1/3}} - a_3 \frac{Z(Z-1)}{\frac{4}{3}}$$



Empirical binding energy per nucleon curve



theoretical binding energy per nucleon curve (using Liquid drop model concept)

Correction to the Formula

The binding energy formula can be improved by taking into account two effects that do no fit into the simple liquid drop model, but which make sense in terms of a model that provides for nuclear energy levels.

Asymmetry Energy

This effect occurs when the neutrons in a nucleus outnumber the protons, which means that higher energy levels have to be occupied than would be case if N and Z were equal.

Asymmetry Energy

Imagine that the neutrons and protons are in a potential well (the nucleus).

We will assume that the well has approximately equally spaced energy levels.

Let the spacing be ΔE .

Neutrons and protons are fermions (spin ½ particles). So the Pauli exclusion principle allows only 2 p and 2 n in each level.





For a nucleus with a given A, the lowest energy will be when N = Z.

$$(Z - N = 0)$$



If we change a proton to a neutron we increase the energy by $1\Delta E$ from Z-N = 0 case. (Now Z-N = 2)



If we change another proton to a neutron ... we increase the energy by ΔE for a total change of $2\Delta E$ from Z-N = 0 case. (Now Z - N = 4)



Another proton to a neutron... we increase the energy by $3 \Delta E$ for a total change of $5 \Delta E$ from Z - N = 0 case. (Now Z - N = 6) Continuing this, we can find the energy shift for a change in Z - N or N - Z.

		$(N-Z)^2$
Z - N or $N - Z$	Total Energy Shift	$(\Delta E) = \frac{8}{8}$
2	1	0.5
4	2	2
6	5	4.5
8	8	8
10	13	12.5
12	18	18
14	25	24.5
16	32	32
We can approx	imate this energy inc	rease by $\frac{(N-Z)^2}{8}\Delta E$

Asymmetry Energy

It has been found that ΔE decreases with A like A⁻¹. Therefore we can write the asymmetry term as

$$E_{a} = -a_{4} \frac{(N-Z)^{2}}{A} = -a_{4} \frac{(A-2Z)^{2}}{A}$$

Pairing Energy

The last correction term arises from the tendency of proton pairs and neutron pairs to occur. Even-even nuclei are the most stable and hence higher binding energies than would otherwise expected. Thus such nuclei appears as peaks in the empirical curve of binding energy per nucleon. At the other extreme, odd- odd nuclei have both unpaired protons and neutrons and have relatively low binding energies. The pairing energy E_p is positive for even-even nuclei, 0 for odd-even nuclei and even-odd nuclei, and negative for odd-odd nuclei. It seems to vary with A as A^{-3/4}. Hence

$$E_p = (\pm, 0) a_5 / A^{3/4}$$

Semi-Empirical Binding Energy Formula

$$E_b = a_1 A - a_2 A^{2/3} - a_3 \frac{Z(Z-1)}{A^{1/3}} - a_4 \frac{(A-2Z)^2}{A} (\pm, 0) \frac{a_5}{A^{3/4}}$$

A set of coefficients that gives a good fit with the data is as follows:

 $a_1 = 14.1 \text{ MeV}$ $a_2 = 13.0 \text{ MeV}$ $a_3 = 0.595 \text{ MeV}$ $a_4 = 19.0 \text{ MeV}$ $a_5 = 33.5 \text{ MeV}$

Merits of Liquid Drop Model

• The liquid drop model accounts for many of the salient features of nuclear matter, such as the observed binding energies of nuclei and their stability against α and β disintegration as well as nuclear fission.

• The calculation of atomic masses and binding energies can done with good accuracy with the liquid drop model.

Demerits of Liquid Drop Model

- It fails to explain the extra stability of certain nuclei, where the number of protons or neutrons in the nucleus are 2, 8, 20, 28, 50, 82, or 126.
- •It fails to explain the measured magnetic moments of many nuclei
- it also fails to explain the spin of nuclei
- It could not explain the excited states in most of the nuclei.