

CLASS: BTech/IMSC
BRANCH: All/PHYSICS

SUBJECT: MA107 MATHEMATICS - II

FULL MARKS: 25

TIME: 02 Hours

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

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|--|-----|----|----|
| Q.1(a) Find the Wronskian of xe^x and x .
Check whether they are linearly independent or not. | [2] | 1 | 1 |
| Q.1(b) Solve the following differential equation:
$y^{iv} - 3y'' - 4y = 0$. | [3] | 1 | 2 |
| Q.2(a) Find the particular solution of :
$(D^2 - 1)y = \cos 2x + a^x$ | [2] | 1 | 1 |
| Q.2(b) Solve the following differential equation:
$[D - 1]^2 y(x) = e^x \sin 2x$ | [3] | 1 | 2 |
| Q.3 Find the power series solution about $x = 0$ of the differential equation:
$y'' - xy' - y = 0$ | [5] | 2 | 1 |
| Q.4(a) Show that when n is an integer,
$J_{-n}(x) = (-1)^n J_n(x)$ | [2] | 2 | 1 |
| Q.4(b) Express x^3 in terms of Legendre polynomials and hence using orthogonality condition evaluate:
$\int_{-1}^1 x^3 P_3(x) dx$ | [3] | 2 | 2 |
| Q.5 Find the Fourier series representation of a periodic function given by:
$1 - x^2, -\pi < x < \pi$. | [5] | 3 | 3 |

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